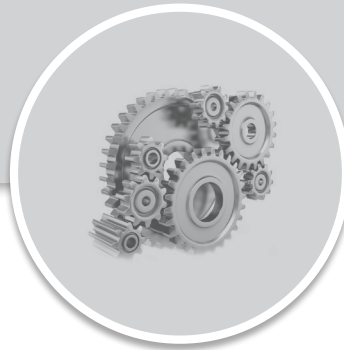


# MECHANICAL ENGINEERING

## Refrigeration & Air-Conditioning



Comprehensive Theory  
*with Solved Examples and Practice Questions*





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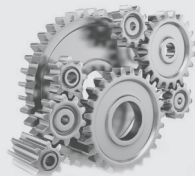
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## Refrigeration & Air-Conditioning

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# Introduction & Basic Concepts of Refrigeration

## 1.1 INTRODUCTION

Refrigeration is a process of removing heat from a confined space so that its temperature is first lowered and then maintained at lower temperature compared to that of the surroundings, i.e. it is a phenomenon by virtue of which one reduces and maintains the temperature of a confined space below that of the surroundings.

In earlier times, refrigeration was achieved by natural means such as evaporative cooling or by use of ice. Ice was generally transported from colder regions, made at night using nocturnal cooling or harvested in winter and stored appropriately in ice houses for use in summer. At present, refrigeration is mostly produced by artificial means.

The device used to produce cold or refrigeration effect is called a refrigeration system or refrigerator. There can be different kinds of refrigeration systems based on working principle. The basic components of a refrigeration system are evaporator, compressor, condenser and expansion valve. In addition to these, there may be a refrigerant accumulator, temperature controller, etc. The refrigerant is a working substance, which circulates through the refrigeration system during its operation.

For example, R134a is the refrigerant used in domestic refrigerators and low-temperature refrigeration systems. R22 is the refrigerant used in window air-conditioning units while ammonia is preferred in large air-conditioning systems. Air is the refrigerant in air-refrigeration cycles which is predominantly used in aircrafts.

Refrigeration cycles are classified mainly into the following:

- Vapour Compression Refrigeration Cycle.
- Vapour Absorption Refrigeration Cycle.
- Air Refrigeration Cycle and Steam-jet Refrigeration Cycle.

### Unit of Refrigeration or Rating for Refrigeration

The definition of refrigeration indicates that refrigeration is nothing but the rate of removal of heat. The SI unit of heat is Joule, the time rate of which is Watt. The unit of refrigeration effect is Watt (W) or kilo Watt (kW).

The standard unit of refrigeration is **ton of refrigeration** or simply ton denoted by the symbol TR. One TR is defined as the amount of heat to be removed from 1000 kg of water at 0° to convert it into ice at 0°C in 24 hours.

$$\text{Thus,} \quad 1 \text{ TR} = \frac{1 \times 2000 \text{ lb} \times 144 \text{ Btu/lb}}{24 \text{ h}} = 12,000 \text{ Btu/h} = 200 \text{ Btu /min}$$

$$\text{But} \quad 1 \text{ Btu} = 1.055 \text{ kJ} \quad \therefore \quad 1 \text{ TR} = 211 \text{ kJ/min} = 3.516 \text{ kW}$$

**NOTE:** In the definition of 1 TR, one ton equals 2000 lb instead of 2240 lb as per the conversion factor. In US, one ton is equal to 2000 lb.

## 1.2 REFRIGERATION AND HEATING LOAD

The refrigeration effect or cooling effect is produced in a refrigeration cycle by the refrigerating equipment. The average rate at which heat is removed from the cold space by the equipment is known as the **cooling load**. It is expressed in kW or TR.

The cooling load on refrigerating equipment results from several different sources. Some of the common sources of heat that contribute to the cooling load on the refrigerating equipments are as follows:

1. Heat entering into the refrigerated space from outside by conduction through the insulated walls.
2. Solar radiations that enter the refrigerated space through transparent glass or other transparent material.
3. Heat on account of warm outside air entering the refrigerated space through open doors or through cracks around windows and doors.
4. Heat emitted by warm products whose temperature is to be lowered to the refrigerated space temperature.
5. Heat emitted by people occupying the refrigerated space. For example, people present in an air-conditioned space or the people working in the cold storages during loading and unloading the goods.
6. Heat emitted by any heat generating equipment installed in the refrigerated space such as lamps, motors, electronic devices, etc.

It is to be noted here that all these sources of heat are not present in every application. The significance of any one heat source with relation to the total cooling load will vary considerably with each application.

In those regions where the atmospheric temperature falls considerably (below  $10^{\circ}\text{C}$ ), especially during winters, heating is needed to keep the rooms warm. The rate of heat to be supplied to such a conditioned space is known as **heating load**. In Western countries, the houses are facilitated with solar heating systems.

## 1.3 CONCEPT OF HEAT ENGINE, REFRIGERATOR AND HEAT PUMP

It is a well-known fact that heat flows in the direction of decreasing temperature, i.e. from a high temperature body to a low temperature body. Such heat transfer occurs in nature without any external aid or device.

### (i) Heat Engine

It is a prime mover that generates heat from the fossil fuel. It works according to the second law of thermodynamics stated by Kelvin and Planck—It is impossible to construct a device that operates continuously in a cycle and produces no effect other than the withdrawal of heat energy from a single reservoir and converts all the heat into useful work. This means that the heat engine (HE) rejects part of the heat available from the heat source while converting it to useful work. As shown in adjacent figure, it takes heat at the rate of  $Q_1$  from the heat source and generates the work at the rate of  $W$  while rejecting heat at the rate of  $Q_2$  to the heat sink. The performance of a heat engine is measured with the help of its 'thermal efficiency' or 'Carnot efficiency' and is mathematically

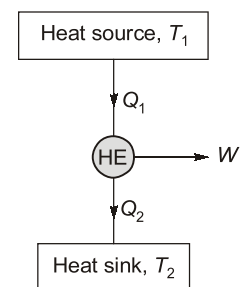


Figure: Heat engine

represented as

$$\eta = 1 - \frac{T_2}{T_1} = 1 - \frac{Q_2}{Q_1}$$

In heat engine, how much work is extracted from a given amount of heat is an important quantity.

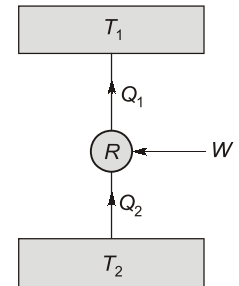
**(ii) Refrigerator**

Reverse heat transfer, i.e. from a body at low temperature to a body at high temperature, is possible only with a special device called refrigerator.

It works according to the second law of thermodynamics stated by Clausius. It is impossible to construct a device that operates in a cycle and produces no effect other than the transfer of heat from a body at low temperature to a body at high temperature without any external aid.

The working principle of the refrigerator (R) is shown in figure. Here  $Q_2$  is the amount of heat removed from the cold space at temperature  $T_2$ .  $Q_1$  is the amount of heat rejected to the environment at temperature  $T_1$  and  $W$  is the net work input to the refrigerator.

In refrigerator, heat extracted from lower temperature is an important quantity.



**Figure: Refrigerator**

**Coefficient of Performance (COP)**

The performance of a device is given by its ability to carry out the assigned task. The performance of a refrigerator is given by its COP. The objective of the refrigerator is to remove heat ( $Q_2$ ) from a closed space. To accomplish this, it needs  $W$  as work input. Therefore, COP of a refrigerator is :

$$\text{COP}_R = \frac{\text{Desired effect}}{\text{Required input}} = \frac{Q_2}{W} \quad \dots (i)$$

But

$$W = Q_1 - Q_2$$

$\therefore$

$$\text{COP}_R = \frac{Q_2}{Q_1 - Q_2} \quad \dots (ii)$$

The COP may be greater than one in many cases, but not necessarily.

If the refrigerator operates on a reversible cycle then,

$$\text{COP}_R = \frac{T_2}{T_1 - T_2}$$

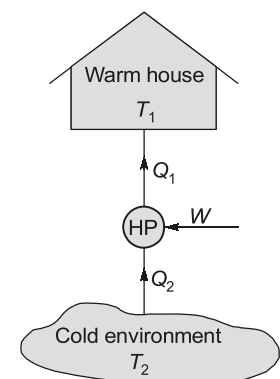
**(iii) Heat Pump**

A heat pump (HP) transfers heat from a low temperature space to a higher temperature space. The objective of a heat pump is to supply heat  $Q_1$  to warm a space as shown in figure. The COP of a heat pump is expressed as the ratio of heat supplied ( $Q_1$ ) to the work input ( $W$ ). Mathematically,

$$\text{COP}_{HP} = \frac{\text{Desired effect}}{\text{Work input}} = \frac{\text{Heating effect}}{\text{Work input}} = \frac{Q_1}{W} \quad \dots (iii)$$

But,

$$W = Q_1 - Q_2$$



**Figure: Heat pump**

$$\therefore (\text{COP})_{\text{HP}} = \frac{Q_1}{Q_2 - Q_2} \quad \dots \text{(iv)}$$

If the heat pump operates on a reversible cycle then,

$$(\text{COP})_{\text{HP}} = \frac{T_1}{T_1 - T_2}$$

Comparing equations (ii) and (iv),

$$\text{COP}_{\text{HP}} = \text{COP}_{\text{R}} + 1 \quad \dots \text{(v)}$$

For fixed rates of  $Q_2$  and  $Q_1$ , equation (iv) shows that the  $\text{COP}_{\text{HP}}$  is always greater than one since the  $\text{COP}_{\text{R}}$  is a positive value. In reality, however, part of  $Q_1$  is lost to the outside air through piping and other devices, and  $\text{COP}_{\text{HP}}$  may drop below one when the outside air temperature is too low.

In heat pump, how much heat is rejected to higher temperature is an important quantity.



- A heat engine is a work producing device whereas, refrigerator and heat pump are work consuming devices.
- A refrigerating machine, that is used for cooling in summer, can be used as a heat pump for heating in winter. This can be done either
  - (i) By rotating the machine to interchange positions of two heat exchangers between space and surroundings, or
  - (ii) By exchanging the functions of the two heat exchangers by the operation of valves. Example, a four way valve used in a window AC.

## 1.4 REVERSED CARNOT CYCLE

It is only theoretical in its conception but serves as an **ideal refrigeration cycle** ever to be achieved in practice. The performance of reversed Carnot cycle is independent of the physical properties of the refrigerant used, so it is valuable as an indication of the highest COP attainable for given conditions.

The  $p$ - $v$  and  $T$ - $s$  diagrams of Carnot cycle using air as refrigerant are shown in figure below.

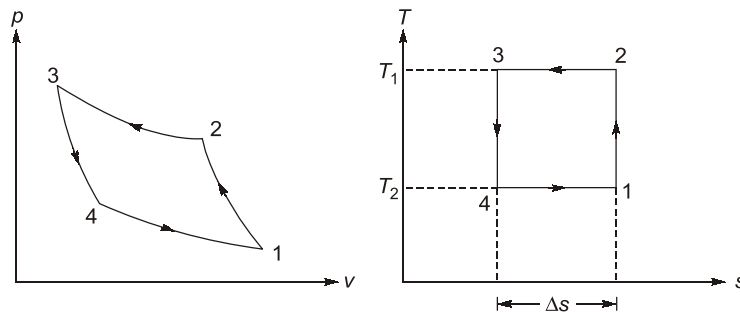


Figure: Reversed Carnot Cycle

Here,

$T_1$  = Temperature to be maintained in refrigerator

$T_2$  = Temperature of the atmosphere to which heat is rejected

In reversed Carnot cycle;

**Process 1-2:** Isentropic compression

**Process 2-3:** Isothermal reversible heat rejection

**Process 3-4:** Isentropic expansion

**Process 4-1:** Isothermal reversible heat addition

From first law for cyclic processes,

$$\oint \delta Q = \oint \delta W$$

If  $W_{\text{net}}$  denotes net work input to the refrigerator then

$$W_{\text{net}} = \text{Heat rejected} - \text{Heat absorbed}$$

$$\begin{aligned} W_{\text{net}} &= Q_r - Q_a = T_2 (s_2 - s_3) - T_1 (s_1 - s_4) \\ &= T_2 \Delta s - T_1 \Delta s = (T_2 - T_1) \Delta s \end{aligned}$$

Thus,

$$(\text{COP})_{\text{rev. Carnot}} = \frac{Q_a}{W} = \frac{T_1 (s_1 - s_4)}{(T_2 - T_1) \Delta s} = \frac{T_1 \Delta s}{(T_2 - T_1) \Delta s} = \frac{T_1}{T_2 - T_1}$$

A high COP is desirable because it indicates that for a required amount of refrigeration, small amount of work is required.

Low value of  $T_2$  will make COP high. High value of  $T_1$  increases the numerator and decreases the denominator and therefore increases the coefficient of performance. The value of  $T_1$  has more pronounced effect upon COP than  $T_2$ . The effects of  $T_1$  and  $T_2$  on COP are shown in figure.

The curve 'a' shows the effect of  $T_1$  on COP when  $T_2$  is constant and the curve 'b' shows the effect of  $T_2$  on COP when  $T_1$  is constant.

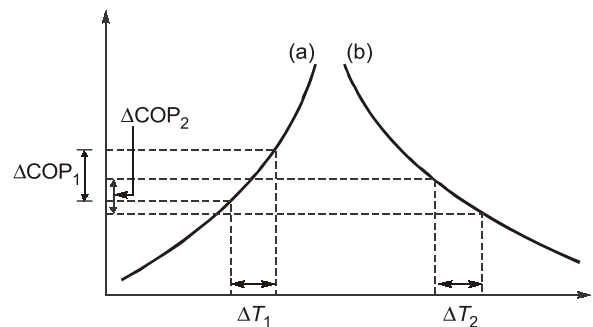
It can be observed from the figure that, if

$$\Delta T_1 = \Delta T_2$$

then,

$$\Delta \text{COP}_1 > \Delta \text{COP}_2$$

Although, the reversed Carnot cycle is most efficient between the fixed temperature limits and is therefore useful as a criterion of perfection, it possesses undesirable characteristics because isentropic process of the cycle requires high speed while the isothermal process requires an extremely low speed. This variation in flow of air (or any other refrigerant) is not practicable.



**EXAMPLE : 1.1**

A refrigeration system operates on reversed Carnot cycle between the temperature limits – 23°C and 45°C. For a refrigerating capacity of 10 TR,

- (a) the COP of the system is 3.67
- (b) the COP of the system is 4.67.
- (c) the heat rejected from the system per hour is 161 MJ nearly.
- (d) the power required by the system is 7.5 kW. [MSQ]

**Solution: (a, c)**

(i)

$$\begin{aligned} \text{COP}_R &= \frac{T_1}{T_2 - T_1} = \frac{273 - 23}{(273 + 45) - (273 - 23)} \\ &= \frac{250}{318 - 250} = 3.67 \end{aligned}$$

(ii) Also,

$$\text{COP}_R = \frac{\text{Refrigerating effect}}{\text{Work input}}$$

∴

$$\text{Work input} = \frac{10 \times 211 \times 60}{3.67} = 34332 \text{ kJ/h}$$

$$\begin{aligned}\text{Heat rejected} &= \text{Refrigerating effect per hour} + \text{Work input per hour} \\ &= (10 \times 211 \times 60) + 34332 \\ &= 160932 \text{ kJ/h} \approx 161 \text{ MJ/h}\end{aligned}$$

$$(iii) \quad \text{Power required} = \frac{34332}{3600} = 9.536 \text{ kW}$$

**EXAMPLE : 1.2**

A refrigerator works on a reversed Carnot cycle. This unit requires 1.5 kW power for every one TR of refrigeration at  $-23^\circ\text{C}$ . If this device is now used as a heat pump, then the corresponding COP will be \_\_\_\_\_. [Correct upto 1 decimal place]

**Solution:**

$$T_1 = -23^\circ\text{C} = 250 \text{ K}$$

$$(i) \quad \text{For refrigerator:} \quad \text{COP}_R = \frac{\text{Refrigerating effect}}{\text{Work done}} = \frac{1 \times 3.516}{1.5} = 2.34$$

$$(ii) \quad \text{Also,} \quad \text{COP}_R = \frac{T_1}{T_2 - T_1} = \frac{250}{T_2 - 250}$$

$$2.34 = \frac{250}{T_2 - 250}$$

$$\text{or} \quad T_2 = 356.6 \text{ K}$$

For heat pump :

$$\begin{aligned}\text{Heat rejected or supplied to a space at } T_2 &= \text{Heat absorbed} + \text{Work done} \\ &= 3.516 + 1.5 = 5.01 \text{ kW}\end{aligned}$$

$$\therefore \quad \text{COP}_{\text{HP}} = \frac{\text{Heat rejected}}{\text{Work done}} = \frac{5.01}{1.5} = 3.3$$

$$\text{Alternatively,} \quad \text{COP}_{\text{HP}} = 1 + \text{COP}_R = 1 + 2.34 = 3.34 \approx 3.3$$

**NOTE**



For the purpose of heating, it is far more economical to use a heat pump rather than an electrical resistance heater. Suppose, if "W" be the work input in electric resistance heater, then its heat output will be "W" only whereas, in case of heat pump, if W be the work input then heat output will be more than W as described below.

$$\text{COP}_{\text{HP}} = \frac{Q_H}{W}$$

$$\Rightarrow \quad Q_H = W + Q_L$$

Though, the initial cost of heat pump will be high, but in the long run it is more economical compared to electric resistance heater.

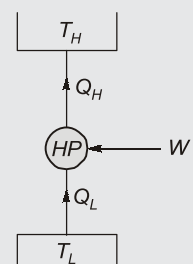


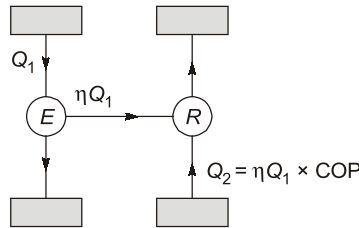
Figure: Heat pump

**EXAMPLE : 1.3**

A heat engine of efficiency ' $\eta$ ' runs a refrigerator of COP ' $C$ '. The COP of the combined refrigerating machine is

- (a)  $\eta C$  (b)  $\frac{1}{\eta C}$   
(c)  $C + \frac{1}{\eta}$  (d)  $\eta + \frac{1}{C}$

**Solution: (a)**



$$\text{Combined COP} = \frac{\text{Heat extracted}}{\text{Heat supplied}} = \frac{\eta Q_1 \times \text{COP}}{Q_1} = \eta C$$



**OBJECTIVE BRAIN TEASERS**

- Q.1** A refrigerator has a second law efficiency of 30%, and heat is removed from the refrigerated space at a rate of 850 kJ/min. If the space is maintained at 0°C while the surrounding air temperature is 36°C. The power required by the refrigerator is \_\_\_\_\_. [Correct upto 1 decimal place]
- Q.2** The Joule-Thomson coefficient for a refrigerant which is to be used in vapour compression refrigeration system should be  
(a) positive (b) negative  
(c) zero (d) infinite
- Q.3** A reversible heat engine operates between the temperature limits  $T_1$  and  $T_2$  and has an efficiency  $\eta$ . If a reversible refrigeration cycle operates between same temperature limits then its COP is  
(a)  $\frac{1}{\eta} - 1$  (b)  $\frac{1}{\eta} + 1$   
(c)  $\frac{1}{\eta}$  (d)  $1 - \frac{1}{\eta}$
- Q.4** The required horsepower per ton refrigeration for a Carnot refrigerator operating between temperature limits 37°C and -23°C is  
(a) 0.94 (b) 1.13  
(c) 0.785 (d) 1.32
- Q.5** A room is kept warm with a system consisting of an electric heater and a heat pump operating on reversed carnot cycle, both supplying equal amount of heat. Heat pump operates between temperature limits of -23°C and 27°C. The COP of the combined heating system is  
(a) 1.32 (b) 1.43  
(c) 1.61 (d) 1.71
- Q.6** A heat pump working on a reversed carnot cycle has a COP of 5 for a work input of 1 kW. If it works as a refrigerator then, the refrigerating effect will be  
(a) 1 kW (b) 2 kW  
(c) 3 kW (d) 4 kW
- Q.7** A carnot refrigerator operates between temperatures -13°C and 27°C. It is desired to make the COP equal to 5 by changing temperatures. If the increase (or decrease) in

upper temperature is to be equal to the decrease (or increase) in lower temperature, then the new value of lower temperature will be

- (a) 254.5 K                      (b) 245.7 K  
(c) 265.8 K                      (d) 270.6 K

**Q.8** A reversible refrigerator working between two fixed temperatures

- (a) Has the same COP whatever be the working substance  
(b) Has its COP increased for working substance with higher enthalpy of evaporation  
(c) Has its COP increased for working substance with specific heats  
(d) None of the above

**Q.9** In a certain ideal refrigeration cycle, the COP of heat pump is 5. The cycle under identical conditions running as heat engine will have efficiency as

- (a) 0                                      (b) 0.2  
(c) 0.5                                      (d) 1

**Q.10** The power (kW) per ton of refrigeration is  $N/\text{COP}$ , then  $N$  is equal to \_\_\_\_\_. [Correct upto 1 decimal place]

**Q.11** A Carnot refrigerator works between the temperatures of 200 K and 300 K, if the refrigerator receives 1 kW of heat, the work requirement will be

- (a) 0.5 kW                              (b) 0.67 kW  
(c) 1.5 kW                              (d) 3 kW

**Q.12** The efficiency of a Carnot engine is 0.75, if the direction of cycle is reversed, what will be the value of COP of Carnot refrigerator.

- (a) 0.27                                      (b) 0.33  
(c) 1.27                                      (d) 2.33

**Q.13** When the lower temperature is fixed, how can the COP of a refrigerating machine be improved?

- (a) By raising the higher temperature  
(b) By lowering the higher temperature  
(c) By operating the machine at high speeds  
(d) By operating the machine at low speeds

**Q.14** Which one of the following is correct relation between  $(\text{COP})_{\text{HP}}$  and  $(\text{COP})_{\text{R}}$

- (a)  $(\text{COP})_{\text{HP}} - (\text{COP})_{\text{R}} = 1$   
(b)  $(\text{COP})_{\text{R}} - (\text{COP})_{\text{HP}} = 1$   
(c)  $(\text{COP})_{\text{HP}} + (\text{COP})_{\text{R}} = 1$   
(d)  $(\text{COP})_{\text{HP}} + (\text{COP})_{\text{R}} = 0$

**Q.15** The COP of a heat pump can be increased either by decreasing  $T_H$  by  $\Delta T$  or by increasing  $T_L$  by  $\Delta T$ . The new COP of the heat pump is

- (a) same in both the cases  
(b) highest if  $T_H$  is decreased  
(c) highest if  $T_L$  is increased  
(d) independent of change in  $T_H$  and  $T_L$

**Q.16** COP of a Carnot heat pump operating between  $-3^\circ\text{C}$  and  $27^\circ\text{C}$  is

- (a) 10                                      (b) 9  
(c) 0.111                                      (d) 0.10

**Q.17** If COP of a refrigerator is 5 and efficiency of a heat engine of the same temperature limit is 50%. Then what is the ratio of heat supplied to engine to heat absorbed by the refrigerator from the space

- (a) 2.5                                      (b) 0.4  
(c) 4    (d) 0.25

**Q.18** If an engine of 40% thermal efficiency drives a refrigerator having a coefficient of performance of 5, then the heat input to engine for each kJ of heat removed from the cold body of the refrigerator is

- (a) 0.50 kJ                                      (b) 0.75 kJ  
(c) 1 kJ    (d) 1.25 kJ

**Q.19** A refrigerator works on reversed Carnot cycle producing a temperature of  $-40^\circ\text{C}$ . Work done per  $TR$  is 700 kJ per ten minutes. What is the value of its COP?

- (a) 3    (b) 4.5  
(c) 5.8    (d) 7.0



**ANSWER KEY**

1. (5.5) 2. (a) 3. (a) 4. (b) 5. (d)  
6. (d) 7. (a) 8. (a) 9. (b) 10. (3.5)  
11. (a) 12. (b) 13. (b) 14. (a) 15. (c)  
16. (a) 17. (b) 18. (a) 19. (a)

**HINTS & EXPLANATIONS**

**1. (5.5) (5.0 to 6.0)**

Given :  $T_H = 36^\circ\text{C} = 309\text{ K}$ ,  $T_L = 0^\circ\text{C} = 273\text{ K}$ ,  
 $Q_2 = 850\text{ kJ/min}$

$$\text{COP}_{\text{rev}} = \frac{T_H}{T_H - T_L} = \frac{309}{36} = 8.58$$

Since,  $\eta_{\text{II}} = \frac{\text{COP}_{\text{act}}}{\text{COP}_{\text{rev}}}$

$$\begin{aligned} \therefore \text{COP}_{\text{act}} &= \text{COP}_{\text{rev}} \cdot \eta_{\text{II}} \\ &= 8.58 \times 0.3 \\ &= 2.574 \end{aligned}$$

Thus, power required,

$$P = \frac{850}{2.574} = 330.2\text{ kJ/min} = 5.5\text{ kW}$$

**3. (a)**

$$\eta = 1 - \frac{T_2}{T_1}$$

$$\Rightarrow \frac{T_2}{T_1} = 1 - \eta$$

$$\therefore \text{COP} = \frac{T_2}{T_1 - T_2} = \frac{1}{\frac{T_1}{T_2} - 1}$$

$$\text{COP} = \frac{1}{\frac{1}{1-\eta} - 1} = \frac{1-\eta}{1-1+\eta}$$

$$\text{COP} = \frac{1-\eta}{\eta} = \frac{1}{\eta} - 1$$

**4. (b)**

For a Carnot refrigerator,

$$\text{COP} = \frac{T_L}{T_H - T_L} = \frac{250}{60} = \frac{25}{6}$$

$$\frac{\dot{Q}}{\dot{W}} = \frac{25}{6}$$

$$\Rightarrow \frac{\dot{W}}{\dot{Q}} = \frac{6}{25}$$

$$1\text{ TR} = 3.5\text{ kW}$$

$$1\text{ HP} = 0.746\text{ kW}$$

$$\frac{\text{HP}}{\text{TR}} = \frac{3.5}{0.746} \times \frac{6}{25} = 1.126$$

**5. (d)**

For heat pump :

$$(\text{COP})_{\text{HP}} = \frac{T_H}{T_H - T_L} = \frac{300}{300 - 250} = 6$$

$$\dot{W}_{\text{HP}} = \frac{\dot{Q}}{(\text{COP})_{\text{HP}}}$$

For electric heater:

$$\dot{Q} = W$$

$$(\text{COP})_{\text{EH}} = 1$$

$$(\text{COP})_{\text{system}} = \frac{\dot{Q} + \dot{Q}}{\dot{Q} + \frac{\dot{Q}}{(\text{COP})_{\text{HP}}}} = \frac{2(\text{COP})_{\text{HP}}}{(\text{COP})_{\text{HP}} + 1}$$

$$= \frac{2 \times 6}{6 + 1} = \frac{12}{7} = 1.71$$

**6. (d)**

$$\begin{aligned} (\text{COP})_{\text{ref}} &= (\text{COP})_{\text{HP}} - 1 \\ &= 5 - 1 = 4 \end{aligned}$$

or  $\frac{\text{R.E.}}{W_{\text{in}}} = 4$

$$\therefore \text{R.E.} = 4 \times 1 = 4\text{ kW}$$

**7. (a)**

For Carnot refrigerator,

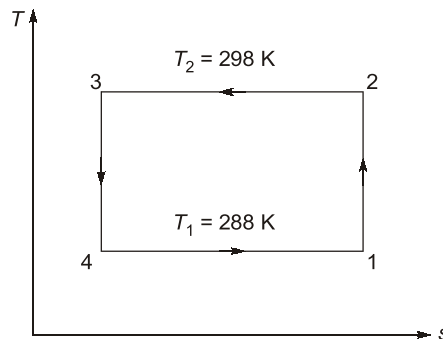
$$\text{COP} = \frac{T_2}{T_1 - T_2}$$



## CONVENTIONAL BRAIN TEASERS

- Q.1 A reversed Carnot cycle working as heat pump is delivering  $4 \times 10^4$  kJ/min to heat the conditioned space and maintaining it at  $25^\circ\text{C}$  when the outside atmospheric air temperature is  $15^\circ\text{C}$ .
- Determine the heat drawn in or pumped into conditioned space from atmospheric air and power required to operate cycle.
  - If the same conditioned space is heated by electric coil heaters, determine consumption of electricity in terms of power consumed.

Solution:



Given:  $Q_R = 4 \times 10^4$  kJ/min,  $T_1 = T_4 = 15^\circ\text{C} = 288$  K,  $T_2 = T_3 = 25^\circ\text{C} = 298$  K

- (i) Heat delivered per minute at  $25^\circ\text{C}$  is given by

$$Q_R = m(s_2 - s_3) \times T_2$$

$$\Rightarrow m(s_2 - s_3) = \frac{4 \times 10^4}{298} = 134.228 \text{ kJ/}^\circ\text{K}$$

Therefore heat absorbed from atmosphere at  $15^\circ\text{C}$

$$Q_A = m(s_1 - s_4) T_1$$

But we know that  $(s_1 - s_4) = (s_2 - s_3)$

$$\begin{aligned} \text{So, } Q_A &= 288 \times 134.228 \\ &= 38657.72 \text{ kJ/min} \end{aligned}$$

$$\begin{aligned} \text{Now, Work done per minute} &= 4 \times 10^4 - 38657.72 \\ &= 1342.28 \text{ kJ/min} \end{aligned}$$

$$\text{So, Power required} = \frac{1342.28}{60} = 22.37 \text{ kW}$$

- (ii) With electric heating coils, for same heat to be delivered,

$$\text{Consumption of electricity} = \frac{4 \times 10^4}{60} = 666.67 \text{ kW}$$

